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## Saving tests by pooling sera—how great are the benefits?

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When a large proportion of a population is negative for a serological factor, it may be possible to reduce the number of tests needed to identify positive individuals by first testing pooled samples and then re-testing individually the sera from any pool that gives a positive result.

If the proportion of negatives in the population is known, the pool size that will minimise the average number of tests needed to get a result for each of a set of sera can be readily established. Suppose sera from  $N$  individuals, each with probability  $p$  of being negative, are pooled in groups of size  $k$ , where  $k$  is a factor of  $N$ . If all the individuals contributing to a pool are negative, only one test will be used. The probability of this happening is  $p^k$ . If, however, the result from a pool is positive, an event occurring with probability  $1 - p^k$ , further  $k$  tests will be needed for that pool. Thus the status of the  $k$  individuals contributing to a pool will be determined by either 1 test, with probability  $p^k$  or  $k + 1$  tests, with probability  $1 - p^k$ . As  $N/k$  is the number of pools, the expected number of tests needed to establish the status of the  $N$  individuals is

$$N/k \times (1 \times p^k + (k + 1) \times (1 - p^k))$$

which equals

$$(N/k) \times (1 + k(1 - p^k)) \quad \dots (A)$$

If  $k$  is not a factor of  $N$ , there will be one or more sera,  $r$  say, left after  $\text{Int}(N/k)$ \* pools of size  $k$  have been made. If these are treated as a separate pool of size  $r$ , the average number of tests needed to examine  $N$  sera will be

$$\text{Int}(N/k) \times (1 + k(1 - p^k)) + 1 \times (1 + r(1 - p^r)) \quad \dots (B)$$

Alternatively, each of the remaining  $r$  sera might be added to one of the pools of size  $k$ , which would make the average number of tests required

$$\text{Int}(N/k) - r \times (1 + k(1 - p^k)) + r \times (1 + (k + 1)(1 - p^{k+1})) \quad \dots (C)$$

As the first practice is probably easier to manage in a laboratory, formula B has been used to calculate the values for Table 1, which shows the average number of tests needed to establish the status of 100 specimens with pool sizes from 2 to 11 for selected values of  $p$ , the proportion of negatives in the popu-

\* $\text{Int}(N/k)$  is the whole number part of the quotient.

Table 1 Average number of tests needed to establish the status of 100 individuals for selected values of  $P$

Proportion of negatives in population ( $P$ )	No. of sera included in each pool ( $k$ )									
	2	3	4	5	6	7	8	9	10	11
0.999	50.2	34.3	25.4	20.5	17.6	15.7	13.8	12.9	11.1	11.1
0.99	52.0	37.0	28.9	24.9	22.8	21.7	20.6	20.6	19.6	20.4
0.95	59.8	48.2	43.5	42.6	43.2	44.8	46.1	48.7	50.1	52.7
0.9	69.0	60.9	59.4	61.0	63.4	66.5	69.1	72.7	75.1	78.0
0.8	86.0	82.5	84.0	87.2	90.2	93.2	95.3	97.9	99.3	100.7
0.6	114.0	112.0	112.0	112.2	112.0	111.5	110.9	110.4	109.4	109.0

Table 2 Ranges of pool sizes which perform relatively well at given values of  $P$

Proportion of negatives in population ( $P$ )	Range of values of $k$ (pool size)	Minimum saving in average no. of tests needed to find positive individuals
0.999	13-90	90%
0.99	7-18	78%
0.98	5-12	70%
0.97	5-8	65%
0.96	4-8	59%
0.95	4-7	55%
0.94	4-7	50%
0.92	3-6	44%
0.9	3-6	36%
0.85	3-5	24%
0.8	3-4	16%
0.75	2-4	6%

lation. This Table shows that if 99% of the population is negative, 10 is the most effective number of sera to include in each pool, and that the method would then, on average, reduce the number of tests used to 1/5 when compared with testing each serum individually. If, on the other hand, only 90% of the population are negative, four would be the best size for each pool. The average number of tests used in these circumstances would be about 3/5 of what would be required if the sera were not pooled. Pooling sera when the proportion of negatives in the population is too low will tend to increase the number of tests needed to above 100. From Table 1 it is also apparent that the precise pool size is not critical. For each proportion of negatives,  $P$ , there is a range of pool sizes about the optimum, all performing similarly.

Generally, of course, the proportion of negatives is not known. The purpose of the tests may be to establish it. It may be, too, that the nature of the test limits the number of sera that can be pooled, or makes some pool sizes more convenient than others. Testing and re-testing may, for instance, be greatly simplified by using specimens from one row of a rack to make each pool. A value of  $k$  based on the rack design may, therefore, be desirable. For these reasons it is useful to know the range of values of  $k$  that perform relatively well for given values of  $P$  (Table 2). A pool size may be chosen from this table using any available knowledge of the proportion of negatives in the population. The expected number of

tests required for a given  $N$ , selected  $k$ , and estimated  $P$  may be calculated using formula A, B, or C, as appropriate.

The procedure should not be used with a test that might fail to detect a weakly positive serum in an otherwise negative pool. It will also be inappropriate if a negative serum can mask a positive by, for instance, an antigen-antibody reaction. If the method is applicable, its usefulness will be largely determined by the proportion of negatives in the population concerned. If positives are rarer than 1 in 100, it will often be beneficial to pool sera as a pool size as small as two will almost halve the number of tests required, and larger pools will produce much greater savings. When positives are more common, up to 1 in 10, say, the value of pooling will depend on the nature of the test. It will be worthwhile only when its cost and complexity outweigh the extra labour involved in making the pools and re-testing the constituents of positive ones individually. For serological factors expected to have a higher incidence than 1 in 10 it is unlikely that pooling will produce a benefit. Indeed, an over-estimate of the proportion of negatives involved may result in the use of more tests than would have been needed to test sera individually in the first place.

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